XI.

Atmospheric Muons and Neutrinos

Astroparticle Physics a.a. 2021/22 Maurizio Spurio Università di Bologna e INFN maurizio.spurio@unibo.it

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Neutrinos from the Cosmos



Once upon a time... GUT

- In the '80 Grand Unified Theories (**GUT**) predicted the proton decay with measurable livetime of the order of τ =10³⁰ y (20 orders of magnitude 1/H_o)
- QUESTION: Which is 1/H_o?
- The proton was thought to decay in (for instance) $p \rightarrow e^+ \pi^0$
- Detector size: 10³ m³, and mass 1kt (=10³¹ p)
- The main background for the detection of proton decay were atmospheric neutrinos interacting inside the experiment
- QUESTION: How many p decays in 1 kt for $\tau = 10^{30}$ y, assuming 100% efficiency?
- Water Cerenkov Experiments (IMB, Kamiokande)
- Tracking calorimeters (NUSEX, Frejus, KGF)
- Result: NO p decay ! But some anomalies on the neutrino measurement!



General problems for $\boldsymbol{\nu}$ detectors

- Low cross section → Large detector volume/mass
- Particle identification
- Energy/momentum measurement
- Direction measurement
- No magnetic field ($v = \overline{v}$)
- Backgrounds







Atmospheric neutrinos



Flux of neutrinos at the surface of the Earth.

Arrow indicate the energy threshold for CC production of the charged lepton

- Big Bang neutrinos
- Neutrinos from the Sun
- Neutrinos from SNe
- Atmospheric neutrinos
- High-energy cosmic neutrinos

The flux of atmospheric muons vs depth

- A sea level, the muon flux is $\Phi \cong 100 \ m^{-2} s^{-1} s r^{-1}$
- Vertical muon intensity vs depth (x-axis, in km.w.e=10⁵ g cm⁻²)
- The shaded area at large depths represents neutrino-induced muons of energy >2 GeV.
- [The figure inset shows the vertical intensity measured under water/ice from nu telescopes.]
- Muons cannot cross more than ≈ 15 km.w.e.



Recipes for the evaluation of the atmospheric flux



Independently from the details of the computation of Φv_{μ} (E), Φv_{e} (E), one can obtain two very robust properties:

• At energies below few GeV, the flux of v_{μ} is approximately twice as large as the *ve*, i.e.:

 $\Phi(v_{\mu})=2\Phi(v_{e})$

• The v_{μ} , v_{e} fluxes are up-down symmetric in zenith ϑ , i.e.: $\Phi_{\nu}(E_{\nu}, \theta) = \Phi_{\nu}(E_{\nu}, \pi - \theta)$

Question 1: why $\Phi(v_{\mu})= 2\Phi(v_{e})$ not hold at higher (>> GeV) energies?

Ingredient 1) The primary CR spectrum



Direct measurements

Indirect measurements



Ingredient 1) Cascade initiated by primary CRs

• Primary CR attenuation as function of X (g cm⁻²) and E

$$\frac{\partial \mathscr{N}_N(E,X)}{\partial X} = -\frac{\mathscr{N}_N(E,X)}{\lambda_{I_N}} + \int_E^\infty \frac{\mathscr{N}_N(E',X)}{\lambda_{I_N}} F_{NN}(E,E') \frac{dE'}{E}$$

• Boundary condition:

$$\mathscr{N}_N(E,0) = \varPhi(E) = KE^{-\alpha}$$

• From Feyman scaling:

$$\mathscr{N}_N(E,X) = \Phi_N(E) \cdot H_N(X)$$

• The dependence on X depends on an effective attenuation length Λ_{N} :

$$H_N(X) = H_N(0) \cdot \exp\left(-\frac{X}{\Lambda_N}\right)$$

$$\Phi_N(E) = K E^{-\alpha} \; .$$

Ingredient 2) p-air cross section



Ingredient 3) Secondary charged multiplicity



Average number of charged hadrons produced in pp (and pp), e+e-, ep collisions versus center of mass energy

Ingredient 2), 3) \rightarrow meson production

• The pion propagation in atmosphere is described by:

$$\frac{\partial \mathscr{N}_{\pi}(E,X)}{\partial X} = -\left(\frac{1}{\lambda_{I_{\pi}}} + \frac{1}{d_{\pi}}\right) \mathscr{N}_{\pi}(E,X)$$

$$+ \int_{0}^{1} \frac{\mathscr{N}_{\pi}(\frac{E}{x^{*}},X)}{\lambda_{I_{\pi}}} \cdot F_{\pi\pi}(x^{*}) \cdot \frac{dx^{*}}{x^{*2}} + \int_{0}^{1} \frac{\mathscr{N}_{N}(\frac{E}{x^{*}},X)}{\lambda_{I_{N}}} \cdot F_{N\pi}(x^{*}) \cdot \frac{dx^{*}}{x^{*2}}$$
(11.15)

• Competition between interaction and decay. The decay length:

$$\frac{1}{d_{\pi}} = \frac{1}{\Gamma c \tau_{\pi^{\pm}} \rho(X)} = \frac{m_{\pi} c^2 h_0}{E c \tau_{\pi^{\pm}} X \cos \theta} = \frac{\varepsilon_{\pi}}{E X \cos \theta}$$

- The pion decay constant ε_{π} =115 GeV.
- Pions start to increase with increasing depth X, reach a maximum and then decrease

• High-energy limit (E>> ε_{π}): the decay term d_{π} can be neglected:

$$\mathcal{N}_{\pi}^{he}(E,X) = \left[\frac{Z_{N\pi}}{1-Z_{NN}} \cdot \frac{\int \Lambda_{\pi}}{\Lambda_{\pi} - \Lambda_{N}} (e^{-X/\Lambda_{\pi}} - e^{-X/\Lambda_{N}})\right] \cdot \underbrace{KE^{-\alpha}}_{KE^{-\alpha}}.$$

(the Z are the the spectrum weighted moments)

• Low-energy limit ($E \cos \vartheta \ll \varepsilon_{\pi}$): we neglect the term $\lambda_{I\pi}$.

$$\mathcal{N}_{\pi}^{le}(E,X) = \left[\frac{Z_{N\pi}}{\lambda_{I_N}} \cdot e^{-X/\Lambda_N} \cdot X\right] \cdot \frac{\cos\theta}{\varepsilon_{\pi}} \cdot KE^{-\alpha+1}$$

• Similar equations hold for other particles with different decay constants:

Table 11.2 Lifetime τ_i and decay constants $\varepsilon_i = mc^2 h_0/c\tau_0$ for secondary particles *i* produced by primary hadrons

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<i>i</i> =	μ^{\pm}	π^{\pm}	π^0	<i>K</i> [±]	D^{\pm}	D^0
τ_i (s)	2.19×10^{-6}	2.60×10^{-8}	8.4×10^{-17}	1.24×10^{-8}	1.04×10^{-12}	4.10×10^{-13}
ε_i (GeV)	1.0	115	3.5×10^{10}	850	4.3×10^{7}	9.2×10^{7}

Ingredient 2), 3) \rightarrow neutrino production

• **Conventional** muons are produced by π and K decays:

- **Prompt** muons by the decay of charmed mesons.
- The muon flux is thus described by the equation:

$$\Phi_{\mu}(E) = \underbrace{KE^{-\alpha}}_{1 + \left(\frac{B_{\pi}E}{\varepsilon_{\pi}}\right)\cos\theta} + \frac{A_{K}}{1 + \left(\frac{B_{K}E}{\varepsilon_{K}}\right)\cos\theta} + \frac{A_{c}}{1 + \left(\frac{B_{c}E}{\varepsilon_{c}}\right)\cos\theta}\right)$$

• The muon neutrino flux follows similarly.

The conventional ν flux: π and K

Solid lines: vertical, dashed lines: venith 60°



 μ^+ + μ^- and ν_{μ} + $\overline{\nu}_{\mu}$ flux from pions and kaons

T. K. Gaisser, Earth Planets Space 58 (2006), 1-5.

Ingredient 4) Solar effects+geomagnetic field

- high precision 3D calculations,
- refined geomagnetic cut-off treatment (also geomagnetic field in atmosphere)
- elevation models of the Earth
- different atmospheric profiles
- geometry of detector effects



The conventional ν flux (Honda)





- The result of one of such calculations: the v flux prediction (Honda) from MC simulations;
- Different models exist;

Question 2: Compute the number of *v* interaction/y for *E_v*>1 GeV in 1 kton detector (ε=1)

Question 3: Explain qualitatively the (ν_{μ}/ν_{e}) ratio

Question 4: Explain qualitatively why the (ν_{μ}/ν_{μ}) ratio increases with energy

Neutrino interactions and cross section



- Different processes for the neutrino interaction on nucleons
- QE: warning to the conservation laws!
- **Question**: why we do not mention the neutrino cross-section on electrons?
- Which is the expected behavior for v+e?



Measurement of atmospheric ν 's



Early measurement of atmospheric v's (<1990)

- Tracking calorimeter: Frejus, Nusex, Soudan (hard to find pictures on the web!)
- Water Cherenkov: IMB, Kamiokande
- Measured the number of neutrino interaction in the detector, separating tracks (= v_{μ}) from showers (= v_{e})



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The golden age (1995-2002): SK and MACRO





- SuperKamiokande (SK) is located in Japan, 1000 m Underground (1996 →)
- MACRO was located at LNGS in Italy (1990-2000)

Super-Kamiokande



- SuperKamiokande (SK) is located in Japan, 1000 m Underground
- Active since 1996
- Filled 50.000 ton water
- 11000 large PMTs +2000 PMTs

25 years of Super-Kamiokande

1996.4 Start data taking

1998 Evidence of atmospheric ν oscillation (SK)

1999.6 K2K started

2001 Evidence of solar ν oscillation (SNO+SK)

2001.7 data taking was stopped for detector upgrade 2001.11 Accident

2002.10 data taking was resumed

2005 Confirm ν oscillation by accelerator ν (K2K)

2006.7 data taking was resumed 2005.10 data taking stopped for full reconstruction

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2019.1 Start

2009 data taking

2018.5 Stop SK-IV











SK-I

SuperKamiokande: v_e



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SuperKamiokande: ν_{μ}







Cherenkov Radiation

 As a charged particle travels, it disrupts the local electromagnetic field (EM) in a medium.

 Electrons in the atoms of the medium will be displaced and polarized by the passing EM field of a charged particle.

 Photons are emitted as an insulator's electrons restore themselves to equilibrium after the disruption has passed.

In a conductor, the EM disruption can be restored without emitting a photon.

 In normal circumstances, these photons destructively interfere with each other and no radiation is detected.

However, when the disruption travels faster
 than light is propagating through the medium, the photons constructively interfere and intensify the observed Cerenkov radiation.



- Threshold velocity $\beta_T = 1/n \rightarrow \theta_T \sim 0$
- Angle of emission (β =1): θ_{max} = arcos(1/n)
- Distribution of emitted photons:

$$\frac{d^2 N}{dx d\lambda} = \frac{2\pi z^2 \alpha}{\lambda^2} \left(1 - \frac{1}{\beta^2 n^2} \right) = \frac{2\pi \cdot z^2 \alpha}{\lambda^2} \sin^2 \theta_C$$
$$\frac{d^2 N}{dx dE} = \frac{z^2 \alpha}{\hbar c} \sin^2 \theta_c.$$

Question 5: Evaluate the number of Cherenkov photons in water in the λ =300-600 nm interval for a relativistic single charged particle

E

dN/dE

The PMTs







The discovery of neutrino masses

- Neutrino are massless in the Standard Model
- Lepton flavour is strictly conserved in SM
- Idea of neutrinos being massive was first suggested by
 B. Pontecorvo, from proposal of neutrino oscillations



$$|\nu_e\rangle$$
, $|\nu_{\mu}\rangle$, $|\nu_{\tau}\rangle$ =Weak Interactions (WI) eigenstats
 $|\nu^1\rangle$, $|\nu^2\rangle$, $|\nu^3\rangle$ =Mass (Hamiltonian) eigenstats

$$\left(\begin{array}{c}\nu_{e}\\\nu_{\mu}\\\nu_{\tau}\end{array}\right) = V_{\rm PNMS} \left(\begin{array}{c}\nu^{1}\\\nu^{2}\\\nu^{3}\end{array}\right)$$

The Pontecorvo-Maki-Nakagawa-Sakata matrix <





...with atmospheric neutrinos



$$P_{\nu_{\mu} \to \nu_{\mu}} = 1 - \sin^2 2\vartheta_{23} \sin^2 \left[1.27 \frac{\Delta m_{23}^2 L}{E_{\nu}} \right]$$

• Δm_{23}^2 , ϑ_{23} \rightarrow from Nature;

- E_{ν} = experimental parameter (energy distribution of neutrino giving a particular configuration of events)
- *L* = experimental parameter (neutrino path length from production to interaction)



v energy/direction: event topology



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cos⊖>0

SuperKamiokande I-IV: results



arXiv:1412.5234v

Discovery of neutrino oscillations





MACRO@ LNGS



- *Liquid scintillator counters*, (3 planes) for the measurement of **time** and **dE/dx**.
- *Streamer tubes* (14 planes), for the measurement of the track position (<1°);
- Detector mass: 5.3 kton
- 1 Up going muons ~ 10⁶ downgoing muons
- Different neutrino topologies



The MACRO neutrino deficits



- Completely different topology w.r.t. SK
- Different experimental technique
- Deformation of the angular distribution w.r.t. expectation
- Missing events from the vertical direction
- Interpretation: oscillations
- The same oscillation parameters!





The Soudan II neutrino deficit



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Why not $v_{\mu} \rightarrow v_{e}$?

• i.e., through the ϑ_{13} angle of the PMNS matrix





Apollonio et al., CHOOZ Coll., Phys.Lett.B466 (1999) 415



The 2015 Nobel Prize

Nobel Prizes and Laureates

Physics Prizes	•	< 2015 >
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▶ Takaaki Kajita

Arthur B. McDonald

All Nobel Prizes in Physics All Nobel Prizes in 2015



The Nobel Prize in Physics 2015 Takaaki Kajita, Arthur B. McDonald



The Nobel Prize in Physics 2015







Photo: K. McFarlane. Queen's University /SNOLAB Arthur B. McDonald

Prize share: 1/2

The Nobel Prize in Physics 2015 was awarded jointly to Takaaki Kajita and Arthur B. McDonald *"for the discovery of neutrino oscillations, which shows that neutrinos have mass"*







Evidence for oscillation of atmospheric neutrinos

The Super-Kamiokande Collaboration



Measurement of the atmospheric neutrino-induced upgoing muon flux using MACRO

The MACRO Collaboration



Now and next... [From E. Lisi (INFN-Bari)]



LBL = Long baseline (few x 100 km); SBL = short baseline (~1 km)

(a) KamLAND reactor [plot]; (b) Borexino [plot], Homestake, Super-K, SAGE, GALLEX/GNO, SNO; (c) Super-K atmosph. [plot], DeepCore, MACRO, MINOS etc.; (d) T2K (plot), NOvA, MINOS, K2K LBL accel.; (e) Daya Bay [plot], RENO, Double Chooz SBL reactor; (f) T2K [plot], MINOS, NOvA LBL accel.; (g) OPERA [plot] LBL accel., Super-K and IC-CD atmospheric.



Now and next... [From E. Lisi (INFN-Bari)]



 $e \rightarrow e (\delta m^2, \theta_{12})$





 $\mu \rightarrow \mu (\Delta m^2, \theta_{23})$



 $\mu \rightarrow \mu (\Delta m^2, \theta_{23})$



Terra cogníta: $\delta m^2 |\Delta m^2|$ $\theta_{12} \theta_{23} \theta_{13}$ $e \rightarrow e (\Delta m^2, \theta_{13})$



 $\mu \rightarrow e (\Delta m^2, \theta_{13}, \theta_{23})$



 $\mu \rightarrow \tau (\Delta m^2, \theta_{23})$



Terra incognita

 $\begin{array}{rl} & 5 \text{ Knowns:} \\ \delta m^2 & \sim 7 \times 10^{-5} \text{ eV}^2 \\ \Delta m^2 & \sim 2 \times 10^{-3} \text{ eV}^2 \\ \sin^2 \theta_{12} & \sim 0.3 \\ \sin^2 \theta_{23} & \sim 0.5 \\ \sin^2 \theta_{13} & \sim 0.02 \end{array}$



5 Unknowns: δ = Dirac CPV phase sign(Δm^2) = ordering octant(θ_{23}) absolute mass scale Dirac/Majorana nature



Atmospheric neutrinos: background for cosmic $\boldsymbol{\nu}$



Solution of question 2)

- The event rate of atmospheric neutrinos can be obtained from Fig. 11.9.
- With a threshold of about 1 GeV, the Φνμ (>1 GeV)=0.65 cm⁻² s⁻¹, and that of Φνe(>1 GeV) a factor of two lower. The neutrino must interact inside the detector to produce a visible event.
- The event rate for T =1 y and for the flavor i= μ ;e is given by

$$N_{\mathbf{v}_i} = \boldsymbol{\Phi}_{\mathbf{v}_i}(> 1 \,\mathrm{GeV}) \cdot \boldsymbol{\sigma}_{\mathbf{v}} \cdot N_T \cdot T$$
,

- $\sigma_v = \sigma_o E$ is the neutrino cross-section. After averaging over neutrinos and aninu's, we have $\sigma_o \approx 0.5 \ 10^{-38} \ cm^2/GeV$
- NT = 6×10^{32} nucleons/ton is the number of target nucleons in 1 tonl,
- T = 3:15 107 s is the number of seconds in 1 year.
- Thus, inserting the numerical values, we obtain

$$N_{\nu_{\mu}} = 66 \text{ kton/y} ; N_{\nu_{e}} = 34 \text{ kton/y} .$$

Solution of question 3)

- At low energy, neutrinos exceed antineutrinos due to the fact that CR protons are more aboundant than neutrons
- Above few hundreds GeV, neutrinos from K decay are more abundant than from pions. Thus, conservation of the strangeness (S) and baryon (B) quantum numbers are responsible for the difference
- Consider the production of charged kaons from pp interactions:
 - K⁺ (B=0, S=1) is produced in association with Λ (B=1, S=-1);
 - K⁻ (B=0, S=-1) requires at least one associated baryon (B=1) **and** an additional strange meson (S=1).
- K^+ are generated much more frequently than K^- because of the associated production with the Λ .

Solution of question 5)

• In water (n=1.33) for z=1 and β =1 the number of photons for energy interval and unit path length is:

$$\frac{d^2 N}{dx dE} = \frac{z^2 \alpha}{\hbar c} \sin^2 \vartheta_c.$$

• With:
$$\cos \theta_c = (1/n) = 0.75 \rightarrow \theta_c = 42^\circ$$

• The $\Delta\lambda$ =(600-300) nm corresponds to Δ E=2 eV, thus

$$\frac{d^2 N}{dx} = \frac{(1/137)}{(197 \text{MeV fm})} \cdot \Delta E \cdot \sin^2 \theta_c = \frac{2 \text{eV} \times (0.67)^2}{27 \cdot 10^3 \times 10^6 \text{eV} \times 10^{-13} \text{cm}} = \frac{330}{\text{cm}}$$